

Assume that $\Sigma = \{0, 1\}$ unless otherwise noted.

1. Create a deterministic TM for the language $L = \{a^n b^n c^n \mid n \geq 0\}$, $\Sigma = \{a, b, c\}$
2. Create a deterministic TM for the language $L = \{w \mid w \text{ contains twice as many 0s as 1s}\}$
3. Show that the class of decidable languages is closed under the operation of concatenation, complementation, and Kleene star.
4. Give a PDA for the language $L = \{a^i b^j c^{2i+1} d^k \mid i, j, k \geq 0\}$, $\Sigma = \{a, b, c, d\}$
5. Give a CFG for the language $L = \{w \in \{0, 1\}^* \mid \text{the number of 0s in } w \text{ is (two times the number of 1s) + 1}\}$
6. Show that the language $L = \{a^n b^n c^n \mid n \geq 0\}$, $\Sigma = \{a, b, c\}$ is not context-free.
7. Show that *CLIQUE* is in *NP*. $CLIQUE = \{ \langle G, k \rangle \mid G \text{ is an undirected graph with a } k\text{-clique} \}$